# CHAPTER - 15 LINEAR INEQUATIONS

## Exercise 15 (A)

#### Question 1.

```
If the replacement set is the set of natural numbers, solve.
```

(i) 
$$x - 5 < 0$$
  
(ii)  $x + 1 < 7$ 

(iii) 
$$3x - 4 > 6$$

# (iv) 4x + 1 > 17

# Solution:

(i) 
$$x - 5 < 0$$
  
  $x - 5 + 5 < 0 + 5$  ......(Adding 5)

$$=> x < 5$$

Required answer = 
$$\{1, 2, 3, 4\}$$

(ii) 
$$x + 1 \le 7 => x + 1 - 1 \le 7 - 1$$
 (Subtracting 1)

$$=> x ≤ 6$$

Required answer = 
$$\{1, 2, 3, 4, 5, 6\}$$

(iii) 
$$3x - 4 > 6$$

$$3x - 4 + 4 > 6 + 4$$
 (Adding 4)

$$=> 3x > 10$$

$$\frac{3x}{3} > \frac{10}{3}$$
 ...(Dividing by 3)

$$=> X > \frac{10}{3}$$

$$=> x > 3\frac{1}{3}$$

(iv) 
$$4x + 1 \ge 17$$

$$=> 4x + 1 - 1 \ge 17 - 1$$
 (Subtracting)

$$=>4x \ge 16$$

$$\Rightarrow \frac{4x}{4} \ge \frac{16}{4}$$
 (Dividing by 4)

## Question 2.

If the replacement set =  $\{-6, -3, 0, 3, 6, 9\}$ ; find the truth set of the following:

(i) 
$$2x - 1 > 9$$

(ii) 
$$3x + 7 < 1$$

(i) 
$$2x - 1 > 9$$

$$\Rightarrow$$
 2x - 1 + 1 > 9 + 1 (Adding 1)

$$\Rightarrow 2x > 10$$

$$\Rightarrow$$
 x > 5 (Dividing by 2)

$$\Rightarrow$$
 x > 5

Required answer =  $\{6, 9\}$ (ii)  $3x + 7 \le 1$  $\Rightarrow 3x + 7 - 7 \le 1 - 7$  (Subtracting 7)  $\Rightarrow 3x \le -6$  $\Rightarrow x \le -2$ Required Answer =  $\{-6, -3\}$ 

## Question 3.

Solve 7 > 3x - 8;  $x \in N$ 

## **Solution:**

$$7 > 3x - 8$$

$$=> 7 - 3x > 3x - 3x - 8$$
 (Subtracting 3x)

$$=> 7 - 7 - 3x > 3x - 3x - 8 - 7$$
 (Subtracting 7)

$$=> -3x > -15$$

$$=> x < 5$$
 (Dividing by -3)

Required Answer =  $\{1, 2, 3, 4\}$ 

Note: Division by negative number reverses the inequality.

#### Question 4.

-17 < 9y - 8;  $y \in Z$ 

## **Solution:**

$$-17 < 9v - 8$$

$$=> -17 + 8 < 9y - 8 + 8$$
 (Adding 8)

$$=> -9 < 9y$$

$$\Rightarrow$$
 -1 < y (Dividing by 9)

Required number =  $\{0, 1, 2, 3, 4, ...\}$ 

## Question 5.

Solve  $9x - 7 \le 28 + 4x$ ;  $x \in W$ 

#### **Solution:**

$$9x - 1 \le 28 + 4x$$

$$=> 9x - 4x - 7 \le 28 + 4x - 4x$$
 (Subtracting 4x)

$$=> 5x - 7 \le 28$$

$$=> 5x - 7 + 7 \le 28 + 7$$
 (Adding 7)

$$=>5x ≤ 35$$

$$=> x \le 7$$
 (Dividing by 5)

Required answer =  $\{0, 1, 2, 3, 4, 5, 6, 7\}$ 

## Question 6.

Solve :  $\frac{2}{3}x + 8 < 12$ ;  $x \in W$ 

Solution:

Sol 
$$\frac{2}{3}x + 8 < 12$$
  

$$\Rightarrow \frac{2}{3}x + 8 - 8 < 12 - 8$$

$$\Rightarrow \frac{2}{3}x < 4$$

$$\Rightarrow \frac{2}{3}x \times \frac{3}{2} < 4 \times \frac{3}{2} \qquad \text{(Multiplying by } \frac{3}{2}\text{)}$$

$$\Rightarrow x < 6$$

$$\therefore \text{ Required answer } = \{0, 1, 2, 3, 4, 5\}$$

#### Question 7.

Solve -5 (x + 4) > 30;  $x \in Z$ 

Solution:

Sol. -5 
$$(x+4) > 30$$
  

$$\Rightarrow \frac{-5(x+4)}{-5} < \frac{30}{-5} ...(Dividing by -5)$$

Note: Division by a negative number reverses the equality

$$\Rightarrow x + 4 < -6$$
  
\Rightarrow x + 4 - 4 < -6 - 4 (Subtracting 4)  
\Rightarrow x < -10

∴ Required Answer = 
$$\{-11, -12, -13, ...\}$$

#### Question 8.

Solve the inquation 8 - 2x > x - 5;  $x \in N$ .

Solution:

Sol. 
$$8 - 2x \ge x - 5$$
;  $x \in \mathbb{N}$   
 $\Rightarrow 8 + 5 \ge 2x + x$   
 $\Rightarrow 13 \ge 3x \Rightarrow 3x \le 13$   
 $\Rightarrow x \le \frac{13}{3} = 4\frac{1}{3}$   
 $x = 1, 2, 3, 4 \ (x \in \mathbb{N})$ 

 $X = 1, 2, 3, 4 (X \in N)$ Solution set =  $\{1, 2, 3, 4\}$ 

## Question 9.

Solve the inequality 18 - 3 (2x - 5) > 12;  $x \in W$ .

Solution:

Sol. 
$$18 - 3 (2x - 5) > 12$$
;  $x \in W$   
 $\Rightarrow 18 - 6x + 15 \quad 33 - 12 > 6x$   
 $\Rightarrow 21 > 6x$   
 $\Rightarrow 6x < 21 \Rightarrow x < \frac{21}{6} + \frac{7}{2} = 3\frac{1}{2}$ 

But 
$$x \in W$$
,  $x = 0, 1, 2, 3$ 

:. Solution set = 
$$\{0, 1, 2, 3\}$$

## Question 10.

Solve :  $\frac{2x+1}{3}$  + 15 < 17; x  $\in$  W.

Solution:

Sol. 
$$\frac{2x+1}{3} + 15 \le 17$$
;  $x \in W$ 

$$\Rightarrow \frac{2x+1}{3} \le 17 - 15 = 2$$

$$\Rightarrow 2x + 1 \le 6 \Rightarrow 2x \le 5$$

$$\Rightarrow x \le \frac{5}{2} = 2\frac{1}{2}$$

But  $x \in W$ 

$$\therefore x = 0, 1, 2$$

 $\therefore$  Solution set is =  $\{0, 1, 2\}$ 

# Question 11.

Solve :  $-3 + x < 2, x \in N$ 

Sol. 
$$-3 + x < 2, x \in \mathbb{N}$$

$$\Rightarrow x < 2 - (-3)$$

$$\Rightarrow x < 2 + 3$$

$$\Rightarrow x < 5$$

$$x = 1, 2, 3, 4$$

$$(\because x \in N)$$

$$\therefore$$
 Solution set = {1, 2, 3, 4}

## Question 12.

Solve: 4x - 5 > 10 - x,  $x \in \{0, 1, 2, 3, 4, 5, 6, 7\}$ 

Solution:

Sol. 
$$4x - 5 > 10 - x$$
,  $x \in \mathbb{N}$ 

$$\Rightarrow 4x + x > 10 + 5$$

$$\Rightarrow 5x > 15$$

$$\Rightarrow x > \frac{15}{5} = 3$$

$$x = 4, 5, 6, 7$$

Solution set =  $\{4, 5, 6, 7\}$ 

## Question 13.

Solve: 15 - 2(2x - 1) < 15,  $x \in Z$ .

**Solution:** 

**Sol.** 
$$15 - 2(2x - 1) < 15, x \in \mathbb{Z}$$

$$\Rightarrow$$
 15 - 4x + 2 < 15

$$\Rightarrow$$
 17 - 4x < 15

$$\Rightarrow -4x < 15 - 17$$

$$\Rightarrow -4x < -2$$

$$\Rightarrow \frac{-4}{-4}x > \frac{-2}{-4} = \frac{1}{2}$$
 (Dividing by -4)

$$\therefore x = 1, 2, 3, 4, 5, \dots$$

$$\therefore$$
 Solution set = {1, 2, 3, 4, 5, ....}

# **Question 14.**

Solve :  $\frac{2x+3}{5} > \frac{4x-1}{2}$ ,  $x \in W$ .

**Sol.** 
$$\frac{2x+3}{5} > \frac{4x-1}{2}, x \in W$$

$$\Rightarrow 2(2x + 3) > 5(4x - 1)$$

$$\Rightarrow$$
 4x + 6 > 20x - 5

$$\Rightarrow$$
 4x - 20x > -5 - 6

$$\Rightarrow -16x > -11$$

$$\Rightarrow x < \frac{-11}{-16}$$
 (Dividing by -16)

$$\Rightarrow x < \frac{11}{16}$$

$$x = 0$$

Solve and graph the solution set on a number line :

Question 1.

x - 5 < -2;  $x \in N$ 

**Solution:** 

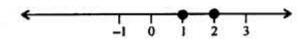
Sol. 
$$x - 5 < -2$$

$$\Rightarrow x - 5 + 5 < -2 + 5$$

(Adding 5 to both sides)

$$\Rightarrow x < 3$$

.. The required graph is :



#### Question 2.

$$3x - 1 > 5$$
;  $x \in W$ 

#### Solution:

**Sol.** 
$$3x-1 > 5$$

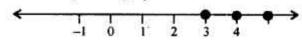
$$\Rightarrow$$
 3x-1+1 > 5+1 (Adding 1 to both sides)

$$\Rightarrow 3x > 6$$

$$\Rightarrow \frac{3x}{3} > \frac{6}{3}$$
 (Dividing both sides by 3)

$$\Rightarrow x > 2$$

.. The required graph is :



#### Question 3.

$$-3x + 12 < -15$$
;  $x \in R$ .

**Sol.** 
$$-3x+12 < -15$$

$$\Rightarrow$$
 -3x+12-12 < -15-12

(Subtracting 12 from both sides)

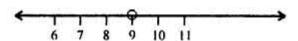
$$\Rightarrow$$
  $-3x < -27$ 

$$\Rightarrow \frac{-3x}{-3} > \frac{-27}{-3}$$
 (Dividing both sides by -3)

Note: Division by a negative number reverses the inequality.

$$\Rightarrow x > 9$$

.. The required graph is :



## Question 4.

7 > 3x - 8;  $x \in W$ 

## **Solution:**

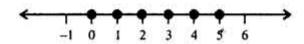
**Sol.** 
$$7 \ge 3x-8$$

$$\Rightarrow$$
 7+8  $\ge$  3x-8+8 (Adding 8 to both sides)

$$\Rightarrow$$
 15  $\geq$  3x

$$\Rightarrow \frac{15}{3} \ge \frac{3x}{3}$$
 (Dividing both sides by 3)

$$\Rightarrow 5 \ge x$$



## Question 5.

$$8x - 8 < -24$$
;  $x \in Z$ 

## **Solution:**

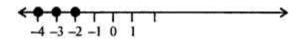
**Sol.** 
$$8x-8 \le -24$$

$$\Rightarrow 8x-8+8 \le -24+8$$

$$\Rightarrow 8x \leq -16$$

$$\Rightarrow \frac{8x}{8} \le \frac{-16}{8}$$
 (Dividing both sides by 8)

$$\Rightarrow x \leq -2$$



## Question 6.

$$8x - 9 > 35 - 3x$$
;  $x \in N$ 

#### Solution:

**Sol.** 
$$8x-9 \ge 35-3x$$

$$\Rightarrow$$
 8x+3x-9  $\geq$  35-3x+3x

(Adding 3x to both sides)

$$\Rightarrow 11x-9 \ge 35$$

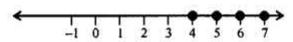
$$\Rightarrow 11x-9+9 \ge 35+9$$

(Adding 9 to both sides)

$$\Rightarrow 11x \ge 44$$

$$\Rightarrow \frac{11x}{11} \ge \frac{44}{11}$$
 (Dividing both sides by 11)

$$\Rightarrow x \ge 4$$



## Question 7.

$$5x + 4 > 8x - 11$$
;  $x \in Z$ 

Solution:

Sol. 
$$5x + 4 > 8x - 11$$

$$\Rightarrow 5x - 5x + 4 > 8x - 5x - 11$$

(Subtracting 5x from both sides)

$$\Rightarrow$$
 4 > 3x - 11

$$\Rightarrow$$
 4 + 11 > 3x - 11 + 11

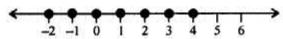
(Adding 11 to both sides)

$$\Rightarrow$$
 15 > 3x

$$\Rightarrow \frac{15}{3} > \frac{3x}{3}$$
 (Dividing both sides by 3)

$$\Rightarrow 5 > x$$

.. The required graph is



## Question 8.

$$\frac{2x}{5}$$
 + 1 < -3; x ∈ R

**Solution:** 

Sol. 
$$\frac{2x}{5} + 1 < -3$$

$$\Rightarrow \frac{2x}{5} + 1 - 1 < -3 - 1$$

(Subtracting 1 from both sides)

$$\Rightarrow \frac{2x}{5} < -4$$

$$\Rightarrow \frac{2x}{5} \times 5 < -4 \times 5$$

(Multiplying both sides by 5)

$$\Rightarrow 2x < -20$$

$$\Rightarrow \frac{2x}{2} < \frac{-20}{2}$$
 (Dividing both sides by 2)

$$\Rightarrow x < -10$$

.. The required graph is :

## Question 9.

$$\frac{x}{2} > -1 + \frac{3x}{4}$$
;  $x \in \mathbb{N}$ 

Solution:

**Sol.** 
$$\frac{x}{2} > -1 + \frac{3x}{4}$$

$$\Rightarrow \frac{x}{2} \times 4 > -1 \times 4 + \frac{3x}{4} \times 4$$

(Multiplying both sides by 4)

$$\Rightarrow 2x > -4+3x$$

$$\Rightarrow$$
 2x-2x > -4+3x-2x

(Subtracting 2x from both sides)

$$\Rightarrow$$
 0 >  $-4+x$ 

$$\Rightarrow$$
 0+4 > -4+4+x (Adding 4 to both sides)

$$\Rightarrow 4 > x$$

.. The required graph is :



## Question 10.

$$\frac{2}{3}$$
 x + 5  $\leq \frac{1}{2}$  x + 6; x  $\in$  W

**Sol.** 
$$\frac{2}{3}x + 5 \le \frac{1}{2}x + 6$$

$$\Rightarrow \frac{2}{3}x \times 6 + 5 \times 6 \le \frac{1}{2}x \times 6 + 6 \times 6$$

(Multiplying both sides by 6)

$$\Rightarrow$$
 4x+30  $\leq$  3x+36

$$\Rightarrow 4x-3x+30 \le 3x-3x+36$$

(Subtracting 3x from both sides)

$$\Rightarrow x+30 \le 36$$

$$\Rightarrow x+30-30 \le 36-30$$

(Subtracting 30 from both sides)

$$x \leq 6$$

.. The required graph is :



## Question 11.

Solve the inequation 5(x - 2) > 4(x + 3) - 24 and represent its solution on a number line.

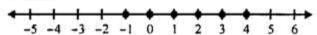
Given the replacement set is {-4, -3, -2, -1, 0, 1, 2, 3, 4}.

**Solution:** 

Sol. 
$$5(x-2) > 4 (x + 3) - 24$$
  
 $\Rightarrow 5x - 10 > 4x + 12 - 24$   
 $\Rightarrow 5x - 4x > 10 - 12$   
 $\Rightarrow x > -2$   
Since replacement set =  $[-4, -3, -2, -1]$ 

Since replacement set =  $\{-4, -3, -2, -1, 0, 1, 2, 3, 4\}$ 

- $\therefore$  Solution set = {-1, 0, 1, 2, 3, 4}
- .. Solution set on a number line is shown below.



## Question 12.

Solve  $\frac{2}{3}$  (x – 1) + 4 < 10 and represent its solution on a number line. Given replacement set is {-8, -6, -4, 3, 6, 8, 12}.

Sol. 
$$\frac{2}{3}(x-1)+4<10$$

$$\Rightarrow \frac{2}{3} (x-1) < 10 - 4$$

$$\Rightarrow \frac{2}{3} (x-1) < 6$$

$$\Rightarrow 2(x-1) < 18$$

$$\Rightarrow x - 1 < 9$$

$$\Rightarrow x - 1 + 1 < 9 + 1$$
 (Adding 1 to both sides)

$$\Rightarrow x < 10$$

Thus x < 10

Since, replacement set =  $\{-8, -6, -4, 3, 6, 8, 12\}$ 

$$\Rightarrow$$
 Solution set = {-8, -6, -4, 3, 6, 8}

## Question 13.

For each inequation, given below, represent the solution on a number line :

(i) 
$$\frac{5}{2} - 2x \ge \frac{1}{2}$$
;  $x \in W$ 

(ii) 
$$3(2x-1) \ge 2(2x+3), x \in Z$$

(iii) 
$$2(4-3x) \le 4(x-5), x \in W$$

(iv) 
$$4(3x + 1) > 2(4x - 1)$$
, x is a negative integer

$$(v)^{\frac{4-x}{2}} < 3, x \in R$$

(vi) 
$$-2(x + 8) \le 8$$
,  $x \in R$ 

$$(i)\ \frac{5}{2}-2x\geq \frac{1}{2}, x\in \mathbb{W}$$

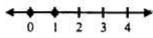
$$\Rightarrow -2x \ge \frac{1}{2} - \frac{5}{2}$$

$$\Rightarrow -2x \ge \frac{-4}{2}$$

$$\Rightarrow -2x > -2$$

$$\Rightarrow x \le 1$$

$$x = \{0, 1\}$$



(ii) 
$$3(2x-1) \ge 2(2x+3), x \in \mathbb{Z}$$

$$\Rightarrow$$
 6x - 3  $\geq$  4x + 6, x  $\in$  Z

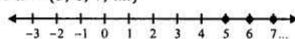
$$\Rightarrow$$
 6x - 4x  $\geq$  6 + 3

$$\Rightarrow 2x \ge 9$$

$$\Rightarrow x \ge \frac{9}{2}$$

$$\Rightarrow x \ge 4\frac{1}{2}$$

$$x = \{5, 6, 7, ....\}$$



(iii) 
$$2(4-3x) \le 4(x-5), x \in W$$

$$8 - 6x < 4x - 20$$

$$\Rightarrow$$
  $-6x - 4x \leq -20 - 8$ 

$$\Rightarrow -10x \le -28$$

$$\Rightarrow 10x \ge 28$$

$$\Rightarrow x \ge \frac{28}{10}$$

$$\Rightarrow x \ge 2.8$$

$$\therefore x = \{3, 4, 5, ....\}$$

(iv) 4(3x + 1) > 2(4x - 1), x is a negative integer

$$\Rightarrow$$
 12x + 4 > 8x - 2

$$\Rightarrow$$
 12x - 8x > -2 - 4

$$\Rightarrow 4x > -6$$

$$\Rightarrow x > \frac{-6}{4}$$

$$\Rightarrow x > -1.5$$

$$\therefore x = \{-1\}$$

$$(v) \frac{4-x}{2} < 3, x \in \mathbb{R}$$

$$\Rightarrow 4-x < 6$$

$$\Rightarrow -x < 6 - 4$$

$$\Rightarrow -x < 2$$

$$\Rightarrow x > -2$$

$$\therefore x > -2$$

$$(vi) -2(x+8) \le 8, x \in R$$

$$-2x - 16 \le 8$$

$$\Rightarrow -2x \leq 8 + 16$$

$$\Rightarrow -2x \leq 24$$

$$\Rightarrow x \ge \frac{-24}{2}$$

$$x \ge -12$$